## Solutions to JEE(Main)-2020

Test Date: 8th January 2020 (Second Shift)

### PHYSICS, CHEMISTRY & MATHEMATICS

Paper - 1

Time Allotted: 3 Hours

Maximum Marks: 300

Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

#### Important Instructions:

- 1. The test is of 3 hours duration.
- 2. This **Test Paper** consists of **75** questions. The maximum marks are **300**.
- 3. There are *three* parts in the question paper A, B, C consisting of **Physics, Chemistry** and **Mathematics** having 25 questions in each part of equal weightage out of which 20 questions are MCQs and 5 questions are numerical value based. Each question is allotted **4 (four)** marks for correct response.
- 4. (Q. No. 01 20, 26 45, 51 70) contains 60 multiple choice questions which have only one correct answer. Each question carries +4 marks for correct answer and –1 mark for wrong answer.
- 5. **(Q. No. 21 25, 46 50, 71 75)** contains 15 Numerical based questions with answer as numerical value. Each question carries **+4 marks** for correct answer. There is no negative marking.
- 6. Candidates will be awarded marks as stated above in **instruction No.3** for correct response of each question. One mark will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer box.
- 7. There is only one correct response for each question. Marked up more than one response in any question will be treated as wrong response and marked up for wrong response will be deducted accordingly as per **instruction 6** above.

### PART - A (PHYSICS)

1. A simple pendulum is being used to determine the vale of gravitational acceleration g at a certain place. The length of the pendulum is 25.0 cm and a stop watch with 1 s resolution measures the time taken for 40 oscillations to be 50 s. The accuracy in g is:

(A) 4.40%

(B) 2.40%

(C) 3.40%

(D) 5.40%

2. A Carnot engine having an efficiency of  $\frac{1}{10}$  is being used as a refrigerator. If the work done on the refrigerator is 10 J, the amount of heat absorbed from the reservoir at lower temperature is:

(A) 99 J

(B) 100 J

(C) 1 J

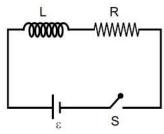
- (D) 90 J
- 3. Consider two charged metallic spheres  $S_1$  and  $S_2$  of radii  $R_1$  and  $R_2$ , respectively. The electric fields  $E_1$  (on  $S_1$ ) and  $E_2$  (on  $S_2$ ) on their surfaces are such that  $E_1/E_2 = R_1/R_2$ . Then the ratio of  $V_1$  (on  $S_1$ ) /  $V_2$  (on  $S_2$ ) of the electrostatic potentials on each sphere is:

(A)  $(R_1/R_2)^2$ 

(B)  $\left(\frac{R_1}{R_2}\right)^3$ 

 $(C) (R_2/R_1)$ 

- (D)  $R_1/R_2$
- 4. As shown in the figure, a battery of emf  $\epsilon$  is connected to an inductor L and resistance R in series. The switch is closed at t = 0. The total charge that flows from the battery, between t = 0 and t =  $t_c$  ( $t_c$  is the time constant of the circuit) is

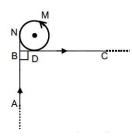


(A)  $\frac{\in L}{eR^2}$ 

(B)  $\frac{\in L}{R^2} \left( 1 - \frac{1}{e} \right)$ 

(C)  $\frac{\in R}{eL^2}$ 

- (D)  $\frac{\in L}{R^2}$
- 5. A very long wire ABADMNDC is shown in figure carrying current I. AB and BC parts are straight, long and at right angle. At D wire forms a circular turn DMND of radius R. AB, BC parts are tangential to circular turn at N and D. Magnetic field at the centre of circle is:



(A)  $\frac{\mu_0 I}{2R}$ 

(B)  $\frac{\mu_0 I}{2\pi R} \left( \pi - \frac{1}{\sqrt{2}} \right)$  A

(C)  $\frac{\mu_0 I}{2\pi R} (\pi + 1)$ 

(D)  $\frac{\mu_0 I}{2\pi R} \left( \pi + \frac{1}{\sqrt{2}} \right)$ 

6. A uniform sphere of mass 500 g rolls without slipping on a plane horizontal surface with its centre moving at a speed of 5.00 cm/s. Its kinetic energy is:

(A) 
$$8.75 \times 10^{-4} \text{ J}$$

(B) 
$$8.75 \times 10^{-3}$$
 J

(D) 
$$1.13 \times 10^{-3}$$
 J

7. In a double-slit experiment, at a certain point on the screen the path difference between the two interfering waves is  $\frac{1}{8}$ th of a wavelength. The ratio of the intensity of light at that point to that at the centre of a bright fringe is:

8. A particle of mass m is dropped from a height h above the ground. At the same time another particle of same mass is thrown vertically upwards from the ground with a speed

If they collide head-on completely inelastically, the time taken for the combined mass to reach the ground, in units of  $\sqrt{\frac{h}{q}}$  is:

(A) 
$$\frac{1}{2}$$

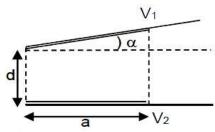
(B) 
$$\sqrt{\frac{1}{2}}$$
 (C)  $\sqrt{\frac{3}{4}}$ 

(C) 
$$\sqrt{\frac{3}{4}}$$

(D) 
$$\sqrt{\frac{3}{2}}$$

- A particle moves such that its position vector  $\vec{r}(t) = \cos \omega \hat{i} + \sin \omega t \hat{j}$  where  $\omega$  is a constant 9. and t is time. Then which of the following statements is true for the velocity  $\vec{v}(t)$  and acceleration  $\vec{a}(t)$  of the particle:
  - (A)  $\vec{v}$  is perpendicular to  $\vec{r}$  and  $\vec{a}$  is directed towards the origin.
  - (B)  $\vec{v}$  and  $\vec{a}$  both are parallel to  $\vec{r}$
  - (C)  $\vec{v}$  is perpendicular to  $\vec{r}$  and  $\vec{a}$  is directed away from the origin.
  - (D)  $\vec{v}$  and  $\vec{a}$  both are perpendicular to  $\vec{r}$
- 10. Consider a mixture of n moles of helium gas and 2n moles of oxygen gas (molecules taken to be rigid) as an ideal gas. It C<sub>P</sub>/C<sub>V</sub> value will be

11. A capacitor is made of two square plats each of side 'a' making a very small angle a between them, as shown in figure. The capacitance will be close to:



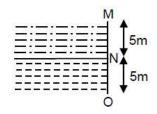
$$(A) \frac{\epsilon_0 a^2}{d} \left( 1 + \frac{\alpha a}{d} \right)$$

(B) 
$$\frac{\epsilon_0}{d} a^2 \left( 1 - \frac{\alpha a}{4d} \right)$$

$$(C) \; \frac{\in_0 \; a^2}{d} \bigg( 1 - \frac{3\alpha a}{2d} \bigg)$$

(D) 
$$\frac{\epsilon_0}{d} a^2 \left( 1 - \frac{\alpha a}{2d} \right)$$

12. Two liquids of densities  $\rho_1$  and  $\rho_2(\rho_2 = 2\rho_1)$  are filled up behind a square wall of inside 10 m as shown in figure. Each liquid has a height of 5 m. The ratio of the forces due to these liquids exerted on upper part MN to that at the lower part NO is (Assume that the liquids are not mixina):



(A) 1/2

(B) 1/4 (C) 2/3(D) 1/3

A plane electromagnetic wave of frequency 25 GHz is propagating in vacuum along the 13. z-direction. At a particular point in space and time, the magnetic field is given by  $\vec{B} = 5 \times 10^{-8} \hat{i}$  T. The corresponding electric field  $\vec{E}$  is (speed of light c = 3 × 10<sup>8</sup> ms<sup>-1</sup>)

(A)  $-1.66 \times 10^{-16} \hat{i} \text{ V/m}$ 

(B) -15 î V/m

(C) 15 î V/m

(D)  $1.66 \times 10^{-16} \hat{i} \text{ V/m}$ 

An electron (mass m) with initial velocity  $\vec{v} = v_0 \hat{i} + v_0 \hat{j}$  is in an electric field  $\vec{E} = -E_0 \hat{k}$ . If  $\lambda_0$ 14. is initial de-Broglie wavelength of electron, its de-Broglie wavelength at time t is given by

 $\text{(A)} \ \frac{\lambda_0}{\sqrt{1+\frac{e^2E_0^2t^2}{m^2v_0^2}}} \qquad \text{(B)} \ \frac{\lambda_0}{\sqrt{2+\frac{e^2E^2t^2}{m^2v_0^2}}} \qquad \text{(C)} \ \frac{\lambda_0\sqrt{2}}{\sqrt{1+\frac{e^2E^2t^2}{m^2v_0^2}}} \qquad \text{(D)} \ \frac{\lambda_0}{\sqrt{1+\frac{e^2E^2t^2}{2m^2v_0^2}}}$ 

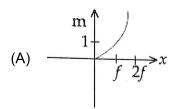
A transverse wave travels on a taut steel wire wit a velocity of v when tension in it is 15.  $2.06 \times 10^4$  N. When the tension is changed to T, the velocity changed to v/2. The value of T is close to:

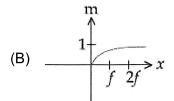
(A)  $10.2 \times 10^2 \text{ N}$ 

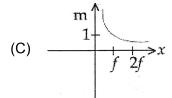
(B)  $30.5 \times 10^4$  N (D)  $2.50 \times 10^4$  N

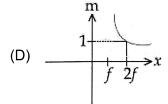
(C) 5.15 × 10<sup>3</sup> N

16. An object is gradually moving away from the focal point of a concave mirror along the axis of the mirror. The graphical representation of the magnitude of linear magnification (m) versus distance of the object from the mirror (x) is correctly given by (Graphs are drawn schematically and are not to scale)

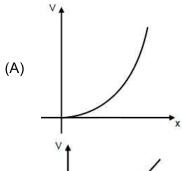




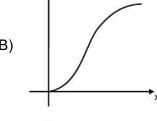


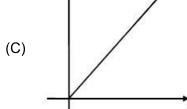


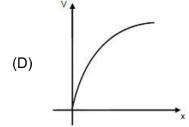
17. A particle of mass m and charge g is released from rest in a uniform electric field. If there is no other force on the particle, the dependence of its speed v on the distance x travelled by it is correctly given by (graphs are schematic and not drawn to scale)



(B)







18. As shown in figure when a spherical cavity (centered at O) of radius 1 is cut out of a uniform sphere of radius R (centred at C), the centre of mass of remaining (shaded) part of sphere is at G, i.e. on the surface of cavity. R can be determined by the equation:

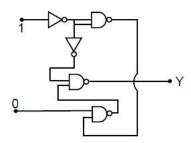


(A) 
$$(R^2 + R + 1) (2 - R) = 1$$

(C) 
$$(R^2 - R + 1)(2 - R) = 1$$

(B) 
$$(R^2 + R - 1) (2 - R) = 1$$
  
(D)  $(R^2 - R - 1) (2 - R) = 1$ 

- (A) 0
- (B) 1
- (C) toggles between 0 and 1
- (D) will not execute



- 20. A galvanometer having a coil resistance 100  $\Omega$  gives a full scale deflection when a current of 1 mA is passed through it. What is the value of the resistance which can convert this galvanometer into a voltmeter giving full scale deflection for a potential difference of 10 V.
  - (A)  $9.9 \text{ k}\Omega$

(B) 7.9 k $\Omega$ 

(C) 10 k $\Omega$ 

(D)  $8.9 \text{ k}\Omega$ 

21.	A ball is dropped form the top of a 100 m high tower on a planet. In the last $\frac{1}{2}$ s before
	hitting the ground, it covers a distance of 19 m. Acceleration due to gravity (in ms <sup>-2</sup> ) near the surface on that planet is

22.	The first member of the Balmer series of hydrogen atom has a wavelength of 6561	Å
	The wavelength of the second member of the Balmer series (in nm) is	

23.	The series combination of two batteries, both of the same emf 10 V, but different internal
	resistance of 20 $\Omega$ and 5 $\Omega$ , is connected to the parallel combination of two resistors 30
	$\Omega$ and R $\Omega$ . The voltage difference across the battery of internal resistance 20 $\Omega$ is zero,
	the value of R (in $\Omega$ ) is $\qquad \qquad$ .

- An asteroid is moving directly towards the centre of the earth. When at a distance of 10 R (R is the radius of the earth) from he earths centre, it has a speed of 12 km/s. Neglecting the effect of earths atmosphere, what will be the speed of the asteroid when it hits the surface of the earth (escape velocity form the earth is 11.2 km/s)? Given your answer to the nearest integer in kilometer/s \_\_\_\_\_.
- 25. Three containers  $C_1$ ,  $C_2$  and  $C_3$  have water at different temperatures. The table below shows the final temperature T when different amounts of water (given in liters) are taken from each container and mixed (assume no loss of heat during the process)

The value of  $\theta$  (in °C to the nearest integer) is \_\_\_\_\_.

## PART -B (CHEMISTRY)

26. The increasing order of the atomic radii of the following elements is:

- (a) C
- (b) O
- (c) F

(e) Br

- (A) (a) < (b) < (c) < (d) < (e)
- (B) (d) < (c) < (b) < (a) < (e)
- (C) (c) < (b) < (a) < (d) < (e)
- (D) (b) < (c) < (d) < (a) < (e)

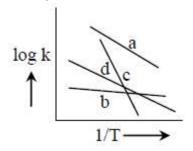
27. Kjeldahl's method cannot be used to estimate nitrogen for which of the following compounds?

(d) Cl

 $(C) C_6 H_5 NO_2$ 

(B)  $C_6H_5NH_2$ (D)  $CH_3CH_2 - C \equiv N$ 

Consider the following plots of rate constant versus  $\frac{1}{T}$  for four different reactions. Which 28. of the following order is correct for the activation energies of these reactions?



(A)  $E_c > E_a > E_d > E_b$ 

(B)  $E_b > E_d > E_c > E_a$ 

(C)  $E_a > E_c > E_d > E_b$ 

(D)  $E_b > E_a > E_d > E_c$ 

29. For the following Assertion and Reason, the correct option is:

**Assertion**: The pH of water increase with increase in temperature.

**Reason**: The dissociation of water into H<sup>+</sup> and OH<sup>-</sup> is an exothermic reaction

- (A) assertion is not true, but reason is true
- (B) both assertion and reason are false
- (C) but the reason is not the correct explanation for the assertion
- (D) both assertion and reason are true, and the reason is the correct explanation for the assertion

30. White phosphorus on reaction with concentrated NaOH solution in an inert atmosphere of CO<sub>2</sub> gives phosphine and compound (X). (X) on acidification with HCl gives compound (Y). The basicity of compound (Y) is:

(A) 2

(B)4

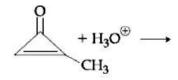
(C) 3

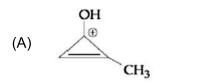
(D) 1

31. The major product [B] in the following sequence is:

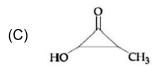
- (C)  $CH_2=C-CH_2CH_2CH_3$  (D)  $CH_3-C-CI$  (D)  $CH_3-C-CI$  (D)  $CH_3-C-CI$
- 32. Among (a) (d), the complexes that can display geometrical isomerism are:
  - (a)  $[Pt(NH_3)_3]CI^{+}$
  - (c)  $[Pt(NH_3)_2CI(NO_2)]$
  - (A) (d) and (a)
  - (C) (b) and (c)

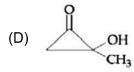
- (b)  $[Pt(NH_3)Cl_5]^-$
- (d)  $[Pt(NH_3)_4ClBr]^{2+}$
- (B) (c) and (d)
- (D) (a) and (b)
- 33. For the following Assertion and Reason, the correct option is:
  - **Assertion:** For hydrogenation reactions, the catalytic activity increases from Group 5 to Group 11 metals with maximum activity shown by Group 7-9 elements.
  - **Reason:** The reactants are most strongly adsorbed on group 7-9 elements. Both assertion and reason are true and the reason is the correct
  - (A) Assertion is not true, but reason is true
  - (B) Both assertion and reason are false
  - (C) but the reason is not the correct explanation for the assertion
  - (D) Both assertion and reason are true, and the reason is the correct explanation for the assertion
- 34. The major product in the following reaction is











35. Among the reactions (a)-(d), the reaction(s) that does/do not occur in the blast furnace during the extraction of iron is/are:

(a) 
$$CaO + SiO_2 \longrightarrow CaSiO_3$$

(b) 
$$3Fe_2O_3 + CO \longrightarrow 2Fe_3O_4 + CO_2$$

(c) 
$$FeO + SiO_2 \longrightarrow FeSiO_3$$

(d) FeO 
$$\longrightarrow$$
 Fe  $+\frac{1}{2}O_2$ 

- 36. A metal (A) on heating in nitrogen gas gives compound B. B on treatment with H<sub>2</sub>O gives a colourless gas which when passed through CuSO<sub>4</sub> solution gives a dark blue-violet coloured solution. A and B respectively, are:
  - (A) Mg and Mg( $NO_3$ )<sub>2</sub>

(B) Na and NaNO<sub>3</sub>

(C) Mg and  $Mg_3N_2$ 

(D) Na and Na<sub>3</sub>N

- 37. Two monomers in maltose are:
  - (A)  $\alpha$ -D-glucose and  $\alpha$ -D-galactose
- (B)  $\alpha$ -D-glucose and  $\beta$ -D-glucose
- (C)  $\alpha$ -D-glucose and  $\alpha$ -D-glucose
- (D)  $\alpha$ -D-glucose and  $\alpha$ -D-Fructose
- 38. The correct order of the calculated spin-only magnetic moments of complexes (A) to (D) is :
  - (a) Ni(CO)<sub>4</sub>

(b)  $[Ni(H_2O)_6]CI_2$ 

(c)  $Na_2[Ni(CN)_4]$ 

(d) PdCl<sub>2</sub>(PPh<sub>3</sub>)<sub>2</sub>

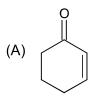
(A) (c)  $\approx$  (d) < (b) < (a)

(B) (a)  $\approx$  (c)  $\leq$  (b)  $\approx$  (d)

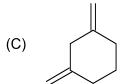
(C) (a)  $\approx$  (c)  $\approx$  (d) < (b)

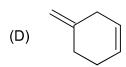
- (D) (c) < (d) < (b) < (a)
- 39. An unsaturated hydrocarbon X absorbs two hydrogen molecules on catalytic hydrogenation, and also gives following reaction:

$$X \xrightarrow[Zn/H_2O]{O_3} A \xrightarrow{[Ag(NH_3)_2]^+} B(3\text{-oxo-hexanedicarboxylic acid}) X will be:$$









- 40. Hydrogen has three isotopes (a), (b) and (c). If the number of neutron(s) in (a), (b) and (c) respectively, are (x), (y) and (z), the sum of (x), (y) and (z) is: (A) 4 (B)3(C) 2 (D) 1 Which of the following compound is likely to show both Frenkel and Schottky defects in 41. its crystalline form? (A) CsCl (B) AgBr (D) KBr (C) ZnS 42. Arrange the following bonds according to their average bond energies in descending order: C-CI, C-Br, C-F, C-I (A) C-F > C-CI > C-Br > C-I(B) C-I > C-Br > C-CI > C-F(C) C-CI > C-Br > C-I > C-F(D) C-Br > C-I > C-CI > C-F43. Preparation of Bakelite proceeds via reactions: (A) Electrophilic substitution and dehydration (B) Condensation and elimination (C) Electrophilic addition and dehydration (D) Nucleophilic addition and dehydration The radius of the second Bohr orbit, in terms of the Bohr radius,  $a_0$ , in  $Li^{2+}$  is 44.
- 45. Among the compounds A and B with molecular formula C<sub>9</sub>H<sub>18</sub>O<sub>3</sub>, A is having higher boiling point the B. The possible structures of A and B are:

- 46. Complexes (ML₅) of metals Ni and Fe have ideal square pyramidal and trigonal bipyramidal geometries, respectively. The sum of the 90°, 120° and 180° L-M-L angles in the two complexes is \_\_\_\_\_\_
- 47. At constant volume, 4 mol of an ideal gas when heated from 300 K to 500 K changes its internal energy by 5000 J. The molar heat capacity at constant volume is \_\_\_\_\_
- 48. In the following sequence of reactions the maximum number of atoms present in molecule 'C' in one plane is

$$A \xrightarrow{\text{Red hot}} B \xrightarrow{\text{CH}_3\text{Cl}(1.\text{eq.})} C \quad (A \text{ is a lowest molecular weight alkyne})$$

- For an electrochemical cell  $Sn(s)|Sn^{2+}$  (aq,  $1M)|Pb^{2+}$  (aq, 1M)|Pb(s) the ratio  $\frac{[Sn^{2+}]}{[Pb^{2+}]}$  when this cell attains equilibrium is \_\_\_\_\_.  $\left(\text{Given}: E^0_{Sn^{2+}|Sn} = -0.14 \text{V}, E^0_{Pb^{2+}|Pb} = -0.13 \text{V}, \frac{2.303 \text{RT}}{F} = 0.06\right)$
- 50. NaClO<sub>3</sub> is used, even in spacecraft, to produce  $O_2$ . The daily consumption of pure  $O_2$  by a person is 492L at 1 atm, 300 K. How much amount of NaClO<sub>3</sub>, in grams, is required to produce  $O_2$  for the daily consumption of a person at 1 atm, 300 K?

$$NaClO_3(s) + Fe(s) \rightarrow O_2(g) + NaCl(s) + FeO(s)$$
  
R = 0.082 L atm mol<sup>-1</sup> K<sup>-1</sup>

## PART-C (MATHEMATICS)

51.	If the 10 <sup>th</sup> term of an A.P. is $\frac{1}{20}$ and its 20 <sup>th</sup>	term is $\frac{1}{10}$ , then the sum of its first 200						
	terms is:	1						
	(A) 100	(B) $50\frac{1}{4}$						
	(C) $100\frac{1}{2}$	(D) 50						
52.	Which of the following statement is a tautology?							
	$(A) \sim (p \land \sim q) \rightarrow p \lor q$	$(B) \sim (p \lor \sim q) \rightarrow p \lor q$						
	(C) $p \lor (\sim q) \rightarrow p \land q$	(D) $\sim (p \lor \sim q) \rightarrow p \land q$						
53.	The mean and variance of 20 observations are found to be 10 and 4, respectively. On rechecking, it was found that an observation 9 was incorrect and the correct observation was 11. Then the correct variance is:							
	(A) 4.02	(B) 3.98						
	(C) 4.01	(D) 3.99						
54.	The mirror image of the point (1, 2, 3) i	n a plane is $\left(-\frac{7}{3}, -\frac{4}{3}, -\frac{1}{3}\right)$ . Which of the						
	following points lies on this plane?	(D) (4, 4, 4)						
	(A) (1, -1, 1) (C) (-1, -1, -1)	(B) (1, 1, 1) (D) (–1, –1, 1)						
55.		10, 16) and it has vertices at $(\pm 6, 0)$ then the						
00.	equation of the normal to it at P is:	10, 10, and it has verified at (±0, 0) then the						
	(A) $2x + 5y = 100$	(B) $x + 3y = 58$						
	(C) $3x + 4y = 94$	(D) $x + 2y = 42$						
56.		le, $(x-3)^2 + y^2 = 1$ and it is perpendicular to						
	a line $L_1$ , where $L_1$ is the tangent to the circ	cle, $x^2 + y^2 = 1$ at the point $\left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$ ; then:						
	(A) $c^2 + 7c + 6 = 0$	(B) $c^2 - 6c + 7 = 0$						
	(C) $c^2 + 6c + 7 = 0$	(D) $c^2 - 7c + 6 = 0$						
57.	The area (in sq. units) of the region $\left\{\left(x,y\right)\in R^{2}\leq y\leq 3-2x\right\}$ , is							
	(A) 32	(B) 29						
	(A) $\frac{32}{3}$	3						
	(C) $\frac{31}{3}$	(B) $\frac{29}{3}$ (D) $\frac{34}{3}$						
	` 3	` 3						

- 58. Let S be the set of all functions  $\int:[0,1]\to R$ , which are continuous on [0,1] and differentiable on (0,1). Then for every  $\int$  in S, there exists  $ac \in (0,1)$ , depending on f, such that:
  - (A) |f(c)-f(1)| < (1-c)|f'(c)|
- (B) |f(c)+f(1)| < (1+c)|f'(c)|

(C) |f(c)-f(1)| < |f'(c)|

- (D)  $\frac{f(1)-f(c)}{1-c} = f'(c)$
- 59. Let  $\vec{a} = \hat{i} 2\hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} \hat{j} + \hat{k}$  be two vectors. If  $\vec{c}$  is a vector such that  $\vec{b} \times \vec{c} = \vec{b} \times \vec{a}$  and  $\vec{c} \cdot \vec{a} = 0$ , then  $\vec{c} \cdot \vec{b}$  is equal to:
  - (A)  $-\frac{1}{2}$

(B)  $-\frac{3}{2}$ 

(C) -1

- (D)  $\frac{1}{2}$
- 60. Let  $f:(1,3) \to R$  be a function defined by  $f(x) = \frac{x[x]}{1+x^2}$ , where [x] denotes the greatest integer  $\le x$ . Then the range of f is:
  - $(A)\left(\frac{2}{5},\frac{4}{5}\right]$

(B)  $\left(\frac{2}{5}, \frac{1}{2}\right) \cup \left(\frac{3}{5}, \frac{4}{5}\right]$ 

(C)  $\left(\frac{3}{5}, \frac{4}{5}\right)$ 

- $(D)\left(\frac{2}{5},\frac{3}{5}\right] \cup \left(\frac{3}{4},\frac{4}{5}\right)$
- 61. Let  $\alpha = \frac{-1+i\sqrt{3}}{2}$ . If  $a = \left(1+\alpha\right)\sum_{k=0}^{100}\alpha^{2k}$  and  $b = \sum_{k=0}^{100}\alpha^{3k}$ , then a and b are the roots of
  - the quadratic equation: (A)  $x^2 - 101x + 100 = 0$

(B)  $x^2 - 102x + 101 = 0$ 

(C)  $x^2 + 102x + 101 = 0$ 

- (D)  $x^2 + 101x + 100 = 0$
- 62.  $\lim_{x\to 0} \frac{\int_0^x t \sin(10t) dt}{x}$  is equal to:
  - (A) 0

(B)  $\frac{1}{10}$ 

(C)  $-\frac{1}{5}$ 

- (D)  $-\frac{1}{10}$
- 63. The system of linear equations

$$\lambda x + 2y + 2z = 5$$

$$2\lambda x + 3y + 5z = 8$$

$$4x + \lambda y + 6z = 10$$
 has:

(A) no solution when  $\lambda = 8$ 

- (B) infinitely many solutions when  $\lambda = 2$
- (C) no solution when  $\lambda = 2$

(D) a unique solution when  $\lambda = -8$ 

- 64. If  $\alpha$  and  $\beta$  be the coefficients of  $x^4$  and  $x^2$  respectively in the expansion of  $\left(x+\sqrt{x^2-1}\right)^6+\left(x-\sqrt{x^2-1}\right)^6$ , then:
  - (A)  $\alpha + \beta = -30$

(B)  $\alpha - \beta = 60$ 

(C)  $\alpha - \beta = -132$ 

- (D)  $\alpha + \beta = 60$
- 65. The differential equation of the family of curves,  $x^2 = 4b(y+b), b \in R$ , is:
  - (A) xy'' = y'

(B)  $x(y')^2 = x - 2yy'$ 

(C)  $x(y')^2 = x + 2yy'$ 

- (D)  $x(y')^2 = 2yy' x$
- 66. The length of the perpendicular from the origin, 0n the normal to the curve,  $x^2 + 2xy 3y^2 = 0$  at the point (2, 2) is:
  - (A)  $2\sqrt{2}$

(B)  $4\sqrt{2}$ 

(C)  $\sqrt{2}$ 

- (D) 2
- 67. If  $A = \begin{pmatrix} 2 & 2 \\ 9 & 4 \end{pmatrix}$  and  $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ , then  $10A^{-1}$  is equal to:
  - (A) 4I A

(B) A - 6I

(C) A - 4I

- (D) 6I A
- 68. Let A and B be two events such that the probability that exactly one of them occurs is  $\frac{2}{5}$  and the probability that A or B occurs is  $\frac{1}{2}$ , then the probability of both of them occur together is:
  - (A) 0.01

(B) 0.10

(C) 0.20

- (D) 0.02
- 69. If  $I = \int_{1}^{2} \frac{dx}{\sqrt{2x^3 9x^2 + 12x + 4}}$ , then:
  - (A)  $\frac{1}{16} < l^2 < \frac{1}{9}$

(B)  $\frac{1}{9} < l^2 < \frac{1}{8}$ 

(C)  $\frac{1}{8} < l^2 < \frac{1}{4}$ 

- (D)  $\frac{1}{6} < l^2 < \frac{1}{2}$
- 70. Let S be the set of all real roots of the equation,  $3^{x}(3^{x}-1)+2=|3^{x}-1|+|3^{x}-2|$ . Then S:
  - (A) contains at least four elements
    - (C) is an empty set

- (B) is a singleton
- (D) contains exactly two elements

- 71. Let f(x) be a polynomial of degree 3 such that f(-1) = 10, f(1) = -6, f(x) has a critical point at x = -1 and f'(x) has a critical point at x = 1. Then f(x) has a local minima at  $x = \underline{\hspace{1cm}}$
- 72. Let aline y = mx(m > 0) intersect the parabola,  $y^2 = x$  at a point P, other than the origin. Let the tangent to it at P meet the x axis at the point Q. If area  $(\Delta OPQ) = 4$  sq. units, then m is equal to \_\_\_\_\_.
- 73. The sum  $\sum_{n=1}^{7} \frac{n(n+1)(2n+1)}{4}$  is equal to \_\_\_\_\_\_.
- 74. The number of 4 letter words (with or without meaning) that can be formed from the eleven letters of the word 'EXAMINATION' is \_\_\_\_\_\_.
- 75. If  $\frac{\sqrt{2}\sin\alpha}{\sqrt{1+\cos2\alpha}} = \frac{1}{7}$  and  $\sqrt{\frac{1-\cos2\beta}{2}} = \frac{1}{\sqrt{10}}$ ,  $\alpha,\beta \in \left(0,\frac{\pi}{2}\right)$ , then  $\tan\left(\alpha+2\beta\right)$  is equal to \_\_\_\_\_.

# JEE (Main) – 2020 ANSWERS

#### **PART -A (PHYSICS)**

1.	Α	2.	D	3.	Α	4.	Α
5.	D	6.	Α	7.	D	8.	D
9.	Α	10.	Α	11.	D	12.	В
13.	С	14.	Α	15.	С	16.	D
17.	D	18.	В	19.	Α	20.	Α
21.	8.00 or 2888.00			22.	486	23.	30
24.	16	25.	50				

#### PART -B (CHEMISTRY)

26.	С	27.	С	28.	Α	29.	В
30.	D	31.	D	32.	В	33.	Α
34.	Α	35.	A	36.	С	37.	С
38.	С	39.	D	40.	В	41.	В
42.	Α	43.	A	44.	Α	45.	D
46.	20.00	47.	6.25	48.	13.00	49.	2.15
50.	2130.00						

## PART-C (MATHEMATICS)

51.	С	52.	В	53.	D	54.	В
55.	Α	56.	С	57.	Α	58.	NA
59.	Α	60.	В	61.	В	62.	Α
63.	С	64.	С	65.	С	66.	Α
67.	В	68.	В	69.	В	70.	В
71.	3	72.	0.5	73.	504	74.	2454

75. **1**